

## Discussion #31 4/20/26 – Spring 2026 MATH 54

### Linear Algebra and Differential Equations

#### Problems

1. Answer the following *true* or *false*:

(a) The functions  $y_1(t) = e^{\alpha t} \cos(\beta t)$  and  $y_2(t) = e^{\alpha t} \sin(\beta t)$  are linearly independent.

(b) The polynomial  $r^4 - 2$  has precisely two distinct roots.

(c) The functions

$$y_1 = t \sin(t) \quad \text{and} \quad y_2 = \cos(t)$$

are linearly independent.

2. Find a particular solution of:

(a)  $y'' + 4y = 3x^3$

(b)  $y'' + 4y = \cos(x)$

(c)  $y'' + 4y = \cos(2x)$

3. Find the general form of a particular solution, but do **not** determine the values of the coefficients, of:

(a)  $y'' + 2y' + y = e^{-t} + \cos(t)$ .

(b)  $y^{(4)} + 5y'' + 4y = \sin(x) + \cos(2x)$

(c)  $y^{(4)} - 2y'' + y = x^2 \cos(x)$

4. Solve the initial value problem

$$y'' + 4y = 2x, \quad y(0) = 1, \quad \text{and} \quad y'(0) = 2.$$